

You should know the following Maclaurin series:

$$e^y = \sum_0^{\infty} \frac{y^n}{n!}$$

$$\sin y = \sum_0^{\infty} \frac{(-1)^n y^{2n+1}}{(2n+1)!}$$

$$\frac{1}{1-y} = \sum_0^{\infty} y^n$$

$$\cos y = \sum_0^{\infty} \frac{(-1)^n y^{2n}}{(2n)!}$$

E.g. Find the Maclaurin series for

$$1) \quad \frac{1}{1+x^2} = \frac{1}{1-(-x^2)} \text{ and here } y = -x^2 \quad \frac{1}{1+x^2} = \sum_0^{\infty} (-x^2)^n = \sum_0^{\infty} (-1)^n x^{2n}$$

$$2) \quad \ln(1+x) = \int \frac{dx}{1+x} = \int \sum_0^{\infty} (-x)^n dx = \sum_0^{\infty} (-1)^n \int x^n dx$$

Find the Maclaurin series for

$$e^{-x^2}$$

$$\tan^{-1} x$$

$$\int_0^{1/2} e^{-x^2} dx$$

$$\frac{\sin x^2}{x}$$

$$\frac{e^x - 1 - x}{x}$$

$$\frac{\sin x - x + \frac{x^3}{6}}{x}$$

$$\frac{\cos x - 1}{x}$$

$$\int_0^1 \cos x^2 dx$$